## Checksup

## Mental calculations, finding a percentage of a quantity

You should be able to handle questions such as the following, mentally, without the use of a calculator or any formal procedures.
a) What is $40 \%$ of 55 ?
b) A total of $83 \%$ of 600 schools participate in an LEA appointments pool. How many schools do not participate?
c) VAT at $17.5 \%$ is to be added to the price of $£ 240$ for a TV set. How much VAT is payable?
d) A school's target for their Key Stage 3 pupils is that $65 \%$ of them should achieve at least level 5 in the English national assessment. If one year they have 180 pupils entering, how many must reach level 5 to achieve the target?

## Answers to check-up 20

a) 22 .
b) 102 .
c) $£ 42$.
d) 117 pupils.

## Discussion and explanation of check-up 20

Since $40 \%=\frac{2}{5}$ and we can find a fifth of 55 very easily (11), the simplest approach with (a) is to think of the $40 \%$ as the equivalent fraction (two-fifths), so $40 \%$ of 55 is 22 .

Otherwise, to handle percentage calculations mentally, start from what you know, or can work out easily, and then work your way gradually to the required percentage. A good starting point is often $10 \%$, which, because it's equal to a tenth, is usually very simple to find. For example, in (b), because $83 \%$ participate and so $17 \%$ do not $(100 \%-83 \%=17 \%)$, we need to work out $17 \%$ of 600 . Now $17 \%$ can be made up from $10 \%, 5 \%, 1 \%$ and $1 \%$, all of which I can jot down instantly: $10 \%$ of 600 is $60 ; 5 \%$ is half of that, $30 ; 1 \%$ of 600 is just 6 (1 per 100 ). So $17 \%$ of $600=60+30+6+6=102$. To find the VAT in (c) I would again start with $10 \%$, then halve this to get $5 \%$, and halve this to get $2.5 \%$. Adding these will give $17.5 \%$ : $£ 24+£ 12+£ 6=£ 42$. In (d) we need $65 \%$ of 180 . Here I would make up the $65 \%$ from $50 \%, 10 \%$ and $5 \%: 90+18+9=117$.

This ad hoc method is surprisingly efficient, even with percentage calculations that look unpromising. You can also involve subtraction if it helps. For example, to find $74 \%$ of 294 you do not really need a calculator, because you can work around 75\%:

| $50 \%$ of 294 | $=$ | 147 | (half of 294) |
| :---: | :---: | :---: | :---: |
| $25 \%$ of 294 | = | 73.5 | (half of the 50\%) |
| $75 \%$ of 294 | = | 220.5 | (adding the 50\% and $25 \%, 147.0+73.5$ ) |
| 1\% of 294 | = | 2.94 | (one hundredth) |
| $74 \%$ of 294 | = | 217.56 | ( $75 \%-1 \%$, i.e. $220.50-2.94$ ) |

Notice that to find $1 \%$ of a number you have to divide by 100 . This results in all the figures moving two places to the right in relation to the decimal point. Notice also, when calculating a sum or difference involving decimals, it is
safest to put in extra zeros to ensure that the numbers have the same number of figures after the decimal point (e.g. $147.0+73.5,220.50-2.94$ ).

## Summary of key ideas

- To find a percentage of a quantity, if the percentage required is equivalent to a simple fraction (like $75 \%=\frac{3}{4}, 40 \%=\frac{2}{5}$ ) that can be worked out easily, then use that fraction.

Otherwise, for mental and informal calculations of percentages of a quantity, build up the required percentage from percentages that are easy to calculate, such as $10 \%, 5 \%, 1 \%, 2 \%, 50 \%, 25 \%)$.

## Further practice

Do these questions without using a calculator, by mental and informal, ad hoc methods.
20.1 What is (a) $12.5 \%$ of 160 ? (b) $30 \%$ of 220 ?
20.2 A secondary school's target for English GCSE results is that at least 78\% of its pupils should achieve grade C or above. How many pupils is that out of a cohort of 240 ?
20.3 In a year group of 125 pupils, $40 \%$ achieved level 5 or above in the Key Stage 2 English test and $36 \%$ achieved level 4 . How many pupils did not reach level 4?

